

# Formal and computational models of language evolution

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September 19, 2006

JSSECL 2006

# Conceptualization of language evolution

## prerequisites for evolutionary dynamics

- replication
- variation
- selection

# Linguemes

- “any piece of structure that can be independently learned and therefore transmitted from one speaker to another” (Nettle 1999:5)
- Croft (2000) attributes the name *lingueme* to Haspelmath (Nettle calls them *items*)
- Examples:
  - phonemes
  - morphemes
  - words
  - constructions
  - idioms
  - collocations
  - ...

# Linguemes

- Linguemes are **replicators**
- comparable to genes
- structured configuration of replicators
  - Biology: genotype
  - Linguistics: utterance

**Croft:**

The utterance is the genome!

# Evolution

## Replication

(at least) two modes of lingueme replication:

- acquisition
- priming (Jäger and Rosenbach 2005; Croft and Nettle would perhaps not agree)

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## Variation

- linguistic creativity
- reanalysis
- language contact
- ...

# Evolution

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## Variation

- linguistic creativity
- reanalysis
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- ...

## Selection

- social selection
- selection for learnability
- selection for primability

# Fitness

## learnability/primability

- selection **against complexity**
- selection **against ambiguity**
- selection **for frequency**



## EGT and pragmatics

**Horn strategies:** prototypical meanings tend to go with simple expressions and less prototypical meanings with complex expressions.

(1)

- a. John went to church/jail. (prototypical interpretation)
- b. John went to the church/jail. (literal interpretation)

(2)

- a. I am going to marry you. (no indirect speech act)
- b. I will marry you. (indirect speech act)


(3)


- a. I need a new driller/cooker.
- b. I need a new drill/cook.


# Horn strategies


- simple game:
  - players: speaker and hearer
  - two forms:  $f_0$  (short) and  $f_1$  (long)
  - two meanings:  $m_0$  (frequent) and  $m_1$  (rare)
  - speaker strategies: mappings from meanings to forms
  - hearer strategies: mappings from forms to meanings

# Speaker strategies





•  $S_1 : m_0 \mapsto f_0, m_1 \mapsto f_1$ :  “Horn strategy”

•  $S_2 : m_0 \mapsto f_1, m_1 \mapsto f_0$ :  “anti-Horn strategy”

•  $S_3 : m_0 \mapsto f_0, m_1 \mapsto f_0$ :  “Smolensky strategy”

•  $S_4 : m_0 \mapsto f_1, m_1 \mapsto f_1$ :  “anti-Smolensky strategy”

# Hearer strategies

- $H_1 : f_0 \mapsto m_0, f_1 \mapsto m_1$ :  
 "Horn strategy"
- $H_2 : f_0 \mapsto m_1, f_1 \mapsto m_0$ :  
 "anti-Horn strategy"
- $H_3 : f_0 \mapsto m_0, f_1 \mapsto m_0$ :  
 "Smolensky strategy"
- $H_4 : f_0 \mapsto m_1, f_1 \mapsto m_1$ :  
 "anti-Smolensky strategy"

## Utility of Horn games

- whether communication works depends both on speaker strategy  $S$  and hearer strategy  $H$
- two factors for functionality of communication
  - communicative success (“hearer economy”)

$$\delta_m(S, H) = \begin{cases} 1 & \text{iff } H(S(m)) = m \\ 0 & \text{else} \end{cases}$$

- least effort (“speaker economy”)

$cost(f)$  . . . measure of complexity of expression

## Utility of Horn games

$$u_s(S, H) = \sum_m p_m \times (\delta_m(S, H) - \text{cost}(S(m)))$$

$$u_h(S, H) = \sum_m p_m \times \delta_m(S, H)$$

$p$  . . . probability distribution over meanings

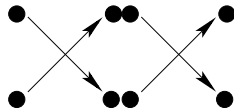
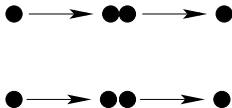
## Utility of Horn game

Let's make up some numbers:

- $p(m_0) = .75$
- $p(m_1) = .25$
- $cost(f_0) = .1$
- $cost(f_1) = .2$

# Utility of Horn game

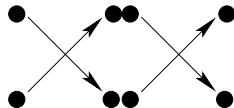
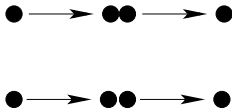
	$H_1$		$H_2$		$H_3$		$H_4$	
$S_1$	.875	1.0	-.125	0.0	.625	.75	.125	.25
$S_2$	-.175	0.0	.825	1.0	.575	.75	.25	.075
$S_3$	.65	.75	.15	.25	.65	.75	.15	.25
$S_4$	.05	.25	.55	.75	.55	.75	.05	.25





# Utility of Horn game

	$H_1$		$H_2$		$H_3$		$H_4$	
$S_1$	.875	1.0	-.125	0.0	.625	.75	.125	.25
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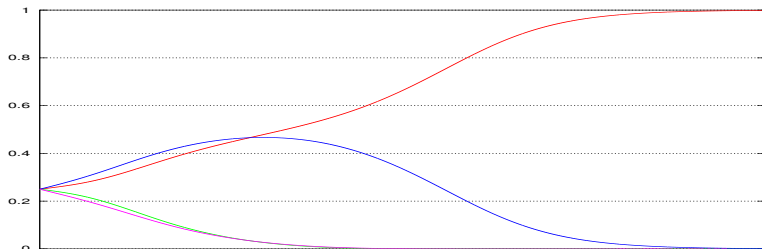
# The problem of equilibrium selection

- both Horn and anti-Horn are evolutionarily stable
- EGT explains the aversion of natural languages against synonymy and ambiguity
- preference for Horn not directly explainable in standard EGT

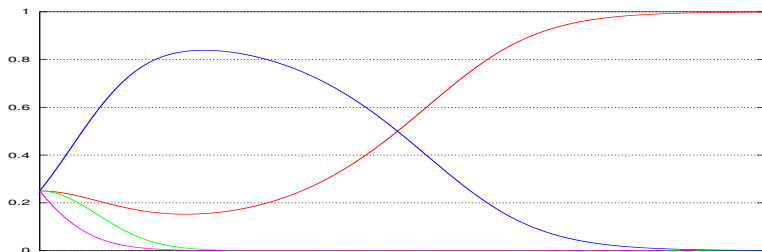
# The problem of equilibrium selection

- rationalistic considerations favor Horn over anti-Horn:
  - Horn strategy is **Pareto efficient** (nobody can do better in absolute terms)
  - Horn strategy **risk dominates** anti-Horn (if you know the population is in an equilibrium but you do not know in which one, going for Horn is less risky than anti-Horn)
- replicator dynamics favors Horn over anti-Horn:
  - complete random state evolves to Horn/Horn
  - basin of attraction of Horn is about 20 times as large as basin of attraction of anti-Horn (numerical approximation—does anybody know how to do this analytically?)

# Dynamics starting from random state



S1 — S2 — S3 — S4

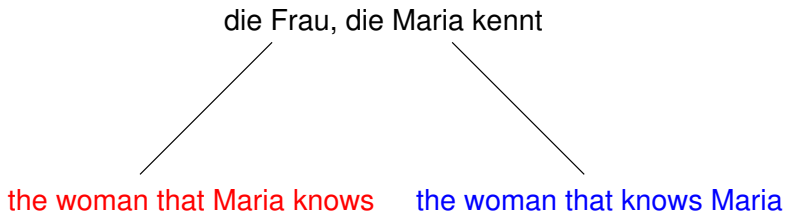


H1 — H2 — H3 — H4

# The evolution of differential case marking

# Ways of argument identification

- transitivity may lead to ambiguity



- three ways out
  - 1 word order
  - 2 agreement
  - 3 **case**

die Frau, die er kennt



the woman that he knows

die Frau, die ihn kennt



the woman that knows him

- Suppose one argument is a pronoun and one is a noun (or a phrase)

{I, BOOK, KNOW}

- both conversants have an interest in successful communication
- case marking (accusative or ergative) is usually more costly than zero-marking (nominative)
- speaker wants to avoid costs



*speaker strategies*

always case mark the object  
(accusative)

always case mark the agent  
(ergative)

case mark the object  
if it is a pronoun

⋮

*hearer strategies*

ergative is agent  
and accusative object

pronoun is agent

pronoun is object

pronoun is agent  
unless it is accusative

⋮

## Statistical patterns of language use

### four possible clause types

	<i>O/p</i>	<i>O/n</i>
<i>A/p</i>	he knows it	he knows the book
<i>A/n</i>	the man knows it	the man knows the book

### statistical distribution (from a corpus of spoken English)

	<i>O/p</i>	<i>O/n</i>
<i>A/p</i>	pp = 198	pn = 716
<i>A/n</i>	np = 16	nn = 75

pn ≫ np

- functionality of speaker strategies and hearer strategies depends on various factors:
  - How often will the hearer get the message right?
  - How many case markers does the speaker need per clause — on average?

# speaker strategies that will be considered

agent is pronoun   agent is noun   object is pronoun   object is noun

e(rgative)	e(rgative)	a(ccusative)	a(ccusative)
e	e	a	z(ero)
e	e	z	a
e	e	z	z
e	z	a	a
...	...	...	...
z	e	z	z
z	z	a	a
z	z	a	z
z	z	z	a
z	z	z	z

- hearer strategies:
  - strict rule: ergative means “agent”, and accusative means “object”
  - elsewhere rules:
    - ① *SO*: “The first phrase is always the agent.”
    - ② *pA*: “Pronouns are agents, and nouns are objects.”
    - ③ *pO*: “Pronouns are objects, and nouns are agents.”
    - ④ *OS*: “The first phrase is always the object.”

## The game of case

- strategy space and utility function are known
- probability of meaning types can be estimated from corpus study
- hard to estimate how the complexity of a case morpheme compares to its benefit for disambiguation from the speaker perspective
- parameterized utility function

$$u(S, H) = \sum_m p_m \times (\delta_m(S, H) - k \times \text{cost}(S(m)))$$

## Utility of case marking

- let us assume  $k = .1$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.90	0.90	0.90	0.90
<i>zzaa</i>	0.90	0.90	0.90	0.90
<i>ezaz</i>	0.85	0.85	0.85	0.85
<i>zeza</i>	0.81	0.81	0.81	0.81
<i>zeaz</i>	0.61	0.97	0.26	0.61
<i>ezzz</i>	0.86	0.86	0.87	0.86
<i>zezz</i>	0.54	0.89	0.54	0.54
<i>zzaz</i>	0.59	0.94	0.59	0.59
<i>zzza</i>	0.81	0.81	0.82	0.81
<i>zzzz</i>	0.50	0.85	0.15	0.50

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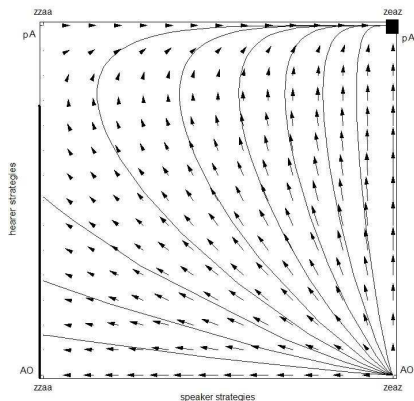
# Utility of case marking

- only one evolutionarily stable state: *zeaz/pA* (*split ergative*)
- very common among Australian aborigines languages

# Non-strict Nash equilibria

Why are non-strict Nash Equilibria unstable?

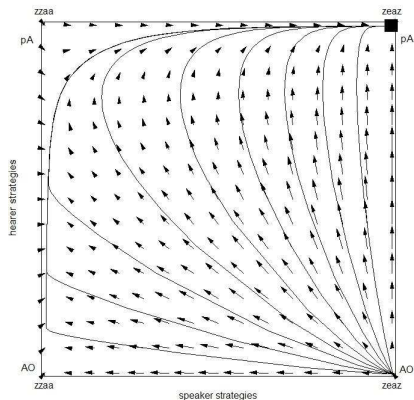
- Dynamics without mutation



# Non-strict Nash equilibria

Why are non-strict Nash Equilibria unstable?

- Dynamics with mutation



## Utility of case marking

If speakers get lazier...

- $k = 0.45$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.550	0.550	0.550	0.550
<i>zzaa</i>	0.550	0.550	0.550	0.550
<i>ezaz</i>	0.458	0.458	0.458	0.458
<i>zeza</i>	0.507	0.507	0.507	0.507
<i>zeaz</i>	0.507	0.863	0.151	0.507
<i>ezzz</i>	0.545	0.538	0.553	0.545
<i>zezz</i>	0.505	0.861	0.148	0.505
<i>zzaz</i>	0.510	0.867	0.154	0.510
<i>zzza</i>	0.539	0.531	0.547	0.539
<i>zzzz</i>	0.500	0.849	0.152	0.500

# Utility of case marking

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# Utility of case marking

... and lazier ...

- $k = 0.53$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.470	0.470	0.470	0.470
<i>zzaa</i>	0.470	0.470	0.470	0.470
<i>ezaz</i>	0.368	0.368	0.368	0.368
<i>zeza</i>	0.436	0.436	0.436	0.436
<i>zeaz</i>	0.483	0.839	0.127	0.483
<i>ezzz</i>	0.473	0.465	0.480	0.473
<i>zezz</i>	0.497	0.854	0.141	0.497
<i>zzaz</i>	0.494	0.850	0.137	0.494
<i>zzza</i>	0.476	0.468	0.484	0.476
<i>zzzz</i>	0.500	0.848	0.152	0.500

## Utility of case marking

... and lazier ...

- $k = 0.53$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.470	0.470	0.470	0.470
<i>zzaa</i>	0.470	0.470	0.470	0.470
<i>ezaz</i>	0.368	0.368	0.368	0.368
<i>zeza</i>	0.436	0.436	0.436	0.436
<i>zeaz</i>	0.483	0.839	0.127	0.483
<i>ezzz</i>	0.473	0.465	0.480	0.473
<i>zezz</i>	0.497	0.854	0.141	0.497
<i>zzaz</i>	0.494	0.850	0.137	0.494
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<i>zzzz</i>	0.500	0.848	0.152	0.500

## Utility of case marking

... and lazier...

- $k = 0.7$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.300	0.300	0.300	0.300
<i>zzaa</i>	0.300	0.300	0.300	0.300
<i>ezaz</i>	0.177	0.177	0.177	0.177
<i>zeza</i>	0.287	0.287	0.287	0.287
<i>zeaz</i>	0.431	0.788	0.075	0.431
<i>ezzz</i>	0.318	0.310	0.326	0.318
<i>zezz</i>	0.482	0.838	0.126	0.482
<i>zzaz</i>	0.457	0.814	0.101	0.457
<i>zzza</i>	0.343	0.335	0.350	0.343
<i>zzzz</i>	0.500	0.848	0.152	0.500



# Utility of case marking

... and lazier...

- $k = 0.7$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.300	0.300	0.300	0.300
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<i>ezaz</i>	0.177	0.177	0.177	0.177
<i>zeza</i>	0.287	0.287	0.287	0.287
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# Utility of case marking

...

- $k = 1$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.000	0.000	0.000	0.000
<i>zzaa</i>	0.000	0.000	0.000	0.000
<i>ezaz</i>	-0.160	-0.160	-0.160	-0.160
<i>zeza</i>	0.024	0.024	0.024	0.024
<i>zeaz</i>	0.340	0.697	-0.016	0.340
<i>ezzz</i>	0.045	0.037	0.053	0.045
<i>zezz</i>	0.455	0.811	0.099	0.455
<i>zzaz</i>	0.394	0.750	0.037	0.394
<i>zzza</i>	0.106	0.098	0.144	0.106
<i>zzzz</i>	0.500	0.848	0.152	0.500

# Utility of case marking

...

- $k = 1$

Speaker strategies	Hearer strategies			
	<i>SO</i>	<i>pA</i>	<i>pO</i>	<i>OS</i>
<i>eezz</i>	0.000	0.000	0.000	0.000
<i>zzaa</i>	0.000	0.000	0.000	0.000
<i>ezaz</i>	-0.160	-0.160	-0.160	-0.160
<i>zeza</i>	0.024	0.024	0.024	0.024
<i>zeaz</i>	0.340	0.697	-0.016	0.340
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<i>zzaz</i>	0.394	0.750	0.037	0.394
<i>zzza</i>	0.106	0.098	0.144	0.106
<i>zzzz</i>	0.500	0.848	0.152	0.500

# Taking stock

zeaz/pA  
split ergative

zzaz/pA  
differential object marking

ezzz/pO  
inverse DOM

zezz/pA  
differential subject marking

zzza/pO  
inverse DSM

zzzz/pA  
no case marking

zzza/pO

zzzz/pA

# Taking stock

zeaz/pA

split ergative

Australian languages

zzaz/pA

differential object marking

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zzzz/pA

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zzza/pO

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Australian languages

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differential object marking

English, Dutch, ...

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zzza/pO

zzzz/pA

# Taking stock

zeaz/pA

split ergative

Australian languages

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zzza/pO

zzzz/pA

# Taking stock

zeaz/pA

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zzzz/pA

no case marking

Chinese, Thai

zzza/pO

zzzz/pA



# Taking stock

zeaz/pA

split ergative

Australian languages

zzaz/pA

differential object marking

English, Dutch, ...

ezzz/pO

inverse DOM

—

zezz/pA

differential subject marking

several caucasian languages

zzza/pO

inverse DSM

Nganasan

zzzz/pA

no case marking

Chinese, Thai

zzza/pO

zzzz/pA

# Taking stock

- only very few languages are not evolutionary stable in this sense  
*zzaa: Hungarian, ezza: Parachi, Yazguljami (Iranian languages), eea: Wangkumara*
- curious asymmetry: if there are two competing stable states, one is common and the other one rare
- similar pattern as with Horn vs. anti-Horn

**Alle equilibria are stable, but  
some equilibria are more stable  
than others.**

**Stochastic EGT**

## Random mutation and stability

- idealizations of standard Evolutionary Game Theory
  - populations are (practically) infinite
  - mutations rate is constant and low
- better model (Young 1993; Kandori, Mailath and Rob 1993)
  - finite population
  - mutation is noisy

## Consequences of finite population model

- every mutation barrier will occasionally be taken
- no absolute stability
- if multiple Strict Nash Equilibria coexist, system will oscillate between them
- some equilibria are more stable than others
- system will spend most of the time in most robustly stable state
- **stochastically stable states**

## A particular model

- discrete time/finite population version of replicator dynamics
- mutations occur rarely (most generations have no mutants at all)
- if mutation occurs, each individual in this generation has same probability to be a mutant
- mutation frequency and mutation rate equal for both populations
- each strategy is equally likely for a mutant (within its population)

## The formulas

$$\frac{\Delta x_i}{\Delta t} = x_i(\tilde{u}_i - \tilde{u}^A) + \sum_j \frac{Z_{ji} - Z_{ij}}{n}$$
$$\frac{\Delta y_i}{\Delta t} = y_i(\tilde{u}_i - \tilde{u}^B) + \sum_j \frac{Z_{ji} - Z_{ij}}{n}$$

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- $x_i$ : frequency of speaker strategy  $i$



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- $Z_{ij}$ : random variable; distributed according to the binomial distribution  $b(p_{ij}, [x_i n])$
- $p_{ij}$ : probability that an  $i$ -individual mutates to strategy  $j$

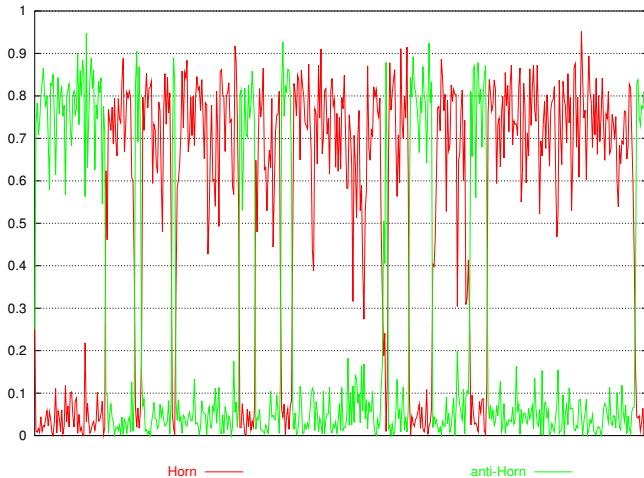
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- $n$ : population size

# A simulation



# Stochastic stability

- punctuated equilibria
- long periods of dynamic stability alternate with short transition periods
- in the long run, more time in Horn state (67% vs. 26% in anti-Horn)
- simulation suggests that Horn is stable while anti-Horn is not
- can this be proved?

# Analytic considerations

- Simple recipes for finding stochastically stable state in  $2 \times 2$  games
- not easily extrapolated to larger games
- basic idea:
  - calculate the height of the invasion barrier of each ESS
  - the ESSs with maximal invasion barrier is stochastically stable



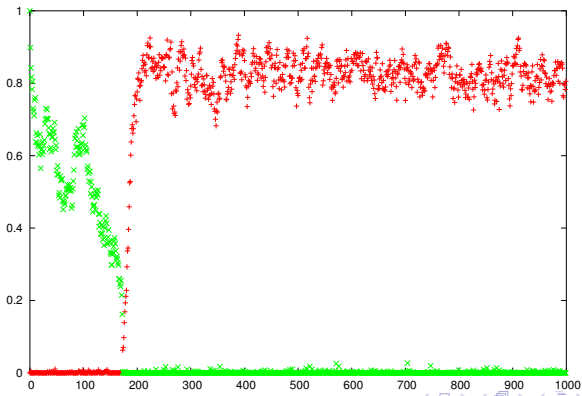
## Analytic considerations

- invasion barrier = amount of mutations necessary to push the system into the basin of attraction of another ESS
- Horn  $\Rightarrow$  anti-Horn: 50%
- anti-Horn  $\Rightarrow$  Horn: 47.5%
- Hence:

**Horn strategy is the only stochastically stable state**

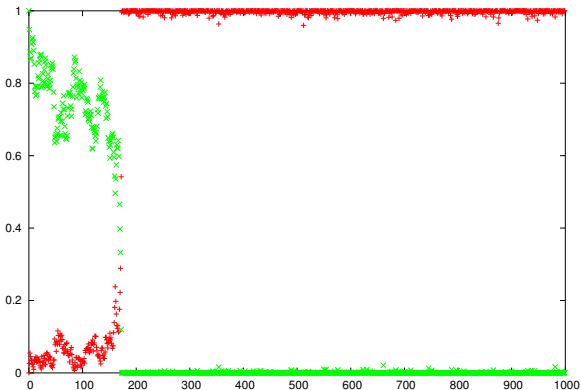
# Stochastic evolution of case marking

- $k = 0.45$
- competition between  $zzaz/pA$  and  $ezzz/pO$
- evolution of speaker population:



# Stochastic evolution of case marking

- $k = 0.45$
- competition between  $zzaz/pA$  and  $ezzz/pO$
- evolution of hearer population:



# Analysis

- invasion barriers:
  - differential object marking: 45.2%
  - inverse differential subject marking: 2.06%

**Differential object marking is stochastically stable;  
inverse differential subject marking is not.**

- likewise, differential subject marking is stochastically stable while inverse differential object marking is not.

# Stochastically stable states

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# Conclusion

- out of  $4 \times 16 = 64$  possible case marking patterns only four are stochastically stable
- vast majority of all languages that fit into this categorization are stochastically stable
- precise numbers are hard to come by though
- linguistic universals can be result of evolutionary pressure in the sense of cultural evolution