# Bioinformatische Methoden in der Historischen Linguistik <br> Aggregating word alignments 

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## From words to languages

- alignment methods give us a measure of distance/similarity between individual words
- these need to be aggregated to get a distance measure between languages
- baseline approach to compute distance between $L_{1}$ and $L_{2}$ :
- compute Levenshtein distance between all 40 translation pairs from $L_{1}$ and $L_{2}$

$$
d\left(L_{1}, L_{2}\right)=\sum_{i=1}^{N} \frac{d\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)}{N}
$$

where $N$ is the number of concepts where we have a word from both languages

- substantial number of missing data; $N$ is often much smaller than 40


## Missing data

- on average we actually only have 35.1 words per language
- if attested loans are excluded, the number goes down to 34.8


number of shared items per language pair


## Evaluation



## Evaluation

- basic problem here: the smaller the sound inventories of the languages compared, the higher is the probability of false positives



## Benchmark: LDND measure

- Wichmann et al.: doubly normalized Levenshtein distance (Levenshtein Distance Normalized and Divided)
- normalization for word length

$$
\begin{equation*}
\operatorname{nld}(x, y) \doteq \frac{d_{\text {Lev }}(x, y)}{\max (I(x), I(y))} \tag{1}
\end{equation*}
$$

- normalization for language specific patterns (including sound inventory size):
- normalization factor $1 / \mu$
- $\mu_{L_{1}, L_{2}}$ : mean of $\left\{n l d(x, y) \mid x \in L_{1}, y \in L_{1},\|x\| \neq\|y\|\right\}$

$$
\begin{aligned}
\operatorname{ldnd}\left(x, y, L_{1}, L_{2}\right) & \doteq \frac{n / d(x, y)}{\mu_{L_{1}, L_{2}}} \\
\operatorname{ldnd}\left(L_{1}, L_{1}\right) & \doteq \frac{\sum_{x \in L_{1}, y \in L_{2}}\left\{\operatorname{ldnd}\left(x, y, L_{1}, L_{2}\right):\|x\|=\|y\|\right\}}{\#\{x, y:\|x\|=\|y\|\}}
\end{aligned}
$$

## Benchmark: LDND measure

English / Swedish

|  | Ei | yu | wi | w3n | tu | fiS | $\ldots$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| yog | 1 | $2 / 3$ | 1 | 1 | 1 | 1 |  |
| du | 1 | $1 / 2$ | 1 | 1 | $1 / 2$ | 1 |  |
| vi | $1 / 2$ | 1 | $1 / 2$ | 1 | 1 | $2 / 3$ |  |
| et | 1 | 1 | 1 | 1 | 1 | 1 |  |
| tvo | 1 | 1 | 1 | 1 | $2 / 3$ | 1 |  |
| fisk | $3 / 4$ | 1 | $3 / 4$ | 1 | 1 | $1 / 2$ |  |

- average LDN along diagonal: 0.56
- average LDN off diagonal: 0.91
- LDND: $0.56 / 0.91=0.61$


## Benchmark: LDND measure



## A bit of information theory

> Swedish fisk $=$ English fish?
> Turkish dört $=$ English dirt?

- first guess is good because the words sound similars and the languages are closely related
- second guess is bad (and wrong) even though the words sound similar because the languages are not related
- If two languages are related, knowing a word from one language reduces the uncertainty about its form in the other language
- Hypothesis: degree of similarity between two languages $\approx$ average amount of information that the form of a word in one language carries about the form of its translation into the other language


## English and Swedish again

- Histogramm: off-diagonal distances
- red line: distance fiS $\sim$ fisk (=4.3)
- relative frequency of off-diagonal entries $\leq 4.3: 0.004$
- can be interpreted as $p$-value for the null hypothesis that the two words are not cognates
- $-\log _{2}(0.004)=7.9$ bit: amout of information that [fisk] carries about [fiS], given the general pattern of phonotactic similarities between unrelated English and Swedish words


## Information theoretic estimate of language similarity

- similarity between two languages: average amount of information that a word from one language carries about its translation
- formally: average binary logarithm of the $p$-values for all Swadesh items in the data base

English/Swedish


English/Turkish


## Information theoretic estimate of language similarity

- formally:
- let $d\left(w_{i}^{L_{1}}, w_{j}^{L_{2}}\right)$ be the normalized Levenshtein distance of the $i$-th word from $L_{1}$ and the $j$-th word from $L_{2}$ and $N$ the number of shared concepts of $L_{1}$ and $L_{2}$.

$$
p v\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)=\frac{\left|\left\{(j, k) \mid i \neq j, d\left(w_{j}^{L_{1}}, w_{k}^{L_{2}}\right)<d\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)\right\}\right|}{N(N-1)}
$$

## How to deal with missing data

- for unrelated languages, $p v\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)$ is just a random variable
- approximately exponentially distributed ( with mean $=\frac{1}{\log 2}$ ):



## How to deal with missing data

- the mean of $N$ exponentially distributed variables is approximately normally distributed ${ }^{1}$
- variance depends on $N$ though




[^0]
## How to deal with missing data

- let $x_{1}, \ldots, x_{N}$ be independent identically distributed random variables with standard deviation $\sigma$

$$
\operatorname{sd}\left(\frac{1}{N} \sum_{i=1}^{N} x_{n}\right)=\frac{\sigma}{\sqrt{N}}
$$

- both mean and variance of the negative (binary) logarithms of the individual $p$-values are $\frac{1}{\log 2}$
- so the following function is standard normally distributed for unrelated languages

$$
\log 2 \sqrt{N}\left(\sum_{i=1}^{N} p v\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)-\frac{1}{\log 2}\right)
$$

## How to deal with missing data

- the following function gives the probability that the degree of similarity that we find between $L_{1}$ and $L_{2}$ is due to chance:

$$
d\left(L_{1}, L_{2}\right)=\operatorname{erfc}\left(\log 2 \sqrt{N}\left(\sum_{i=1}^{N} p v\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)-\frac{1}{\log 2}\right)\right)
$$

- as the complementary error function erfc is monotonically decreasing, we can define the similarity betwen $L_{1}$ and $L_{2}$ as

$$
\operatorname{sim}\left(L_{1}, L_{2}\right)=\sqrt{N}\left(\sum_{i=1}^{N} p v\left(w_{i}^{L_{1}}, w_{i}^{L_{2}}\right)-\frac{1}{\log 2}\right)
$$

## Comparing unweighted and weighted alignment

- same procedure for aggregating word-alignments to language similarities can be applied to weighted alignments
- some results

Levensthein:
German Swabian Cimbrian Dutch Hindi PIE Latin Hungarian Finnish Turkish

| German | 45.7 | 35.2 | 26.7 | 25.8 | 10.1 | 14.9 | 10.9 | 6.8 | 6.0 | 6.9 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Swabian | 35.2 | 46.5 | 22.0 | 21.8 | 10.0 | 13.0 | 11.5 | 7.2 | 6.8 | 6.1 |
| Cimbrian | 26.7 | 22.0 | 42.3 | 20.7 | 11.8 | 10.7 | 9.8 | 5.9 | 6.7 | 6.1 |
| Dutch | 25.8 | 21.8 | 20.7 | 45.7 | 9.5 | 14.0 | 11.2 | 6.9 | 5.7 | 5.1 |
| Hindi | 10.1 | 10.0 | 11.8 | 9.5 | 45.7 | 14.4 | 12.1 | 6.5 | 7.1 | 7.5 |
| PIE | 14.9 | 13.0 | 10.7 | 14.0 | 14.4 | 46.5 | 19.6 | 8.1 | 6.4 | 5.2 |
| Latin | 10.9 | 11.5 | 9.8 | 11.2 | 12.1 | 19.6 | 46.5 | 8.0 | 6.1 | 6.9 |
| Hungarian | 6.8 | 7.2 | 5.9 | 6.9 | 6.5 | 8.1 | 8.0 | 42.7 | 11.5 | 8.5 |
| Finnish | 6.0 | 6.8 | 6.7 | 5.7 | 7.1 | 6.4 | 6.1 | 11.5 | 37.9 | 7.4 |
| Turkish | 6.9 | 6.1 | 6.1 | 5.1 | 7.5 | 5.2 | 6.9 | 8.5 | 7.4 | 45.7 |

weighted alignment:
German Swabian Cimbrian Dutch Hindi PIE Latin Hungarian Finnish Turkish

| German | 42.3 | 36.3 | 31.6 | 29.0 | 12.0 | 16.9 | 12.2 | 7.5 | 7.2 | 6.3 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Swabian | 36.3 | 42.3 | 27.8 | 26.0 | 12.4 | 15.5 | 12.4 | 8.2 | 7.1 | 6.2 |
| Cimbrian | 31.6 | 27.8 | 40.8 | 24.8 | 13.0 | 12.8 | 10.9 | 7.5 | 7.5 | 6.4 |
| Dutch | 29.0 | 26.0 | 24.8 | 41.4 | 11.8 | 16.7 | 12.7 | 7.5 | 5.9 | 5.2 |
| Hindi | 12.0 | 12.4 | 13.0 | 11.8 | 42.9 | 14.6 | 13.3 | 8.1 | 6.9 | 7.2 |
| PIE | 16.9 | 15.5 | 12.8 | 16.7 | 14.6 | 45.8 | 22.6 | 8.3 | 7.7 | 5.2 |
| Latin | 12.2 | 12.4 | 10.9 | 12.7 | 13.3 | 22.6 | 44.2 | 7.4 | 6.3 | 7.5 |
| Hungarian | 7.5 | 8.2 | 7.5 | 7.5 | 8.1 | 8.3 | 7.4 | 42.9 | 12.3 | 9.0 |
| Finnish | 7.2 | 7.1 | 7.5 | 5.9 | 6.9 | 7.7 | 6.3 | 12.3 | 34.3 | 7.0 |
| Turkish | 6.3 | 6.2 | 6.4 | 5.2 | 7.2 | 5.2 | 7.5 | 9.0 | 7.0 | 44.2 |

## Comparison

- applying Neighbor Joining phylogeny induction


Levenshtein alignment
weighted alignment

## The Balto-Slavic languages: Levenshtein alignment



## The Balto-Slavic languages: Weighted alignment



## The Slavic languages: Ethnologue classification



## The Romance languages: Levenshtein alignment



## The Romance languages: Weighted alignment



## The Romance languages: Ethnologue classification



## The Germanic languages: Levenshtein alignment



## The Germanic languages: Weighted alignment



## The Germanic languages: Ethnologue classification



## Tree distances：Robinson－Fould

## The symmetric difference metric




Partitions
\｛ADF｜BCEG\}
\｛DF｜ABCEG\}
\｛BC｜ADEFG\}
Partitions
\｛ADF｜BCEG\}
\｛AD｜BCEFG \}
\｛BC｜ADEFG $\}$ \｛EG｜ABCDF\}

The symmetric difference is the number of partitions that are in one but not both of these lists，in this case 3 ．

## Tree distances: Robinson-Fould

- normalized RF-distance: number of different partitions, divided by the total number of partitions in tree $1+$ total number of partitions in tree 2
- in the example: $\frac{3}{4+3}$


## Tree distances: Quartet distance

- for a quartet of species, there are four possible tree topologies, 3 butterflies and 1 star



## Tree distances: Quartet distance

- quartet distance between two unrooted trees is the number quartets that have a different topology in the two trees


## Tree distances: Quartet distance



- $\binom{7}{4}=35$ quartets in total
- 25 are shared, 10 are different
- normalized qdist: $\frac{10}{35}$


## Tree distances

- Robinson-Fould distance is more intuitive, but quartet distance is more robust

- Robinson-Fould distance: 6; normalized $\frac{6}{8}=0.75$
- quartet distance: 23 ; normalized $\frac{23}{35} \approx 0.66$


## Expert trees

- quality of phylogenetic inference can be evaluated by comparison to expert classifications
- three commonly used classification systems:

1. two-level taxonomy from WALS (World Atlas of Language Structure)
2. multi-level taxonomy from Ethnologue
3. more conservative multi-level taxonomy according to Harald Hammarström

- all three are part of the meta-data in ASJP


## Expert trees and tree distances

- most nodes in the expert trees are multiple branching
- trees that are produced by phylogenetic software are always binary branching
- this leads to misleadingly high tree distances


## Expert trees and tree distances

- suppose the left tree is extracted from the data and the right one is an expert tree

- as the left tree correctly captures all taxa in the right tree, this seems to be a perfect fit
- however:
- normalized Robinson-Fould distance: 0.33
- normalized quartet distance: 0.11


## Expert trees and tree distances

- in practice
- 5,644 languages in ASJP (excluding creoles etc.)
- there 5,641 partitions in every inferred tree
- Ethnologue: 1,803 partitions
- WALS: 391 partitions
- Hammarström: 1,735 partitions
- Robinson-Fould distance to WALS tree will be at least 0.68 , no matter how well the algorithm performs
- minimum quartet distance: not easy to calculate, but also substantial


## Measures of fit

- more realistic measures of goodness of fit:
- Robinson-Fould fit:
$\frac{\text { number of shared partitions }}{\text { total number of partitions in the expert tree }}$
- quartet fit:
number of shared butterflies total number of butterflies in the expert tree
- these measures are always between 0 and 1
- 1 means that all groupings from the expert classification are correctly recovered


## Triplet fit

- pick a triplet of languages $A, B, C$ which has a resolved tree structure $((A, B), C)$ according to the expert tree
- determine predicted distances:

$$
\begin{aligned}
d(\text { Swedish, English }) & =0.486 \\
d(\text { Swedish, Japanese }) & =0.905 \\
d(\text { English, Japanese }) & =0.897
\end{aligned}
$$

- $\quad d(A, B)<\min (d(A, C), d(B, C)) \mapsto$ correct
- otherwise $\mapsto$ incorrect
- triplet fit of a distance measure to an
resolved:

unresolved:
 expert tree: proportion of resolved triplets that come out correct


## Triplet fit

- Wichmann et al. claim that 40 Swadesh items are enough; longer Swadesh lists lead to a decrease in quality according to their methods

- Note: More data is better than less data.


## Some results

- compute 5,644 $\times 5,644$ distance matrices based on Levenshtein alignment vs. weighted alignment
- perform Neighbor-Joining algorithm
- measure fit to expert trees
- Robinson-Fould fit:

|  | Levenshtein | weighted | Aline |
| :--- | ---: | ---: | ---: |
| WALS | 0.624 | 0.639 | 0.622 |
| Ethnologue | 0.485 | 0.490 | 0.477 |
| Hammarström | 0.457 | 0.473 | 0.447 |

## Some results

- quartet fit:

|  | Levenshtein | weighted | ALINE |
| :--- | ---: | ---: | ---: |
| WALS | 0.869 | 0.886 | 0.855 |
| Ethnologue | 0.839 | 0.857 | 0.824 |
| Hammarström | 0.890 | 0.896 | 0.891 |

## Some results

- triangle fit:

|  | Levenshtein | weighted | ALINE |
| :--- | ---: | ---: | ---: |
| WALS | 0.8816 | 0.9055 | 0.8876 |
| Ethnologue | 0.7733 | 0.7980 | 0.7734 |
| Hammarström | 0.7670 | 0.7904 | 0.7699 |

## Some results

- procedure: for $N=100,200,300, \ldots, 1,800$ :
- pick $N$ languages at random
- compute $N \times N$ distance matrices based on Levenshtein vs. weighted alignment
- perform Neighbor Joining algorithm
- measure fit to Hammarström expert tree
- Robinson-Fould fit:



## Some results

- procedure: for $N=100,200,300, \ldots, 1,800$ :
- pick $N$ languages at random
- compute $N \times N$ distance matrices based on Levenshtein vs. weighted alignment
- perform Neighbor Joining algorithm
- measure fit to Hammarström expert tree
- quartet fit:



## Some results

- difference between weighted alignment and Levenshtein alignment for the same data set
- Robinson-Fould fit
qdist-fit: difference between weighted and unweighted alignment

- quartet fit

RF-fit: difference between weighted and unweighted alignment

$\mu=0.023$


[^0]:    ${ }^{1}$ Strictly speaking, it is a Erlang distribution, but for $N>10$ or so, a normal distribution is a reasonable approximation.

