

# Cost-based pragmatic implicatures in an artificial language experiment

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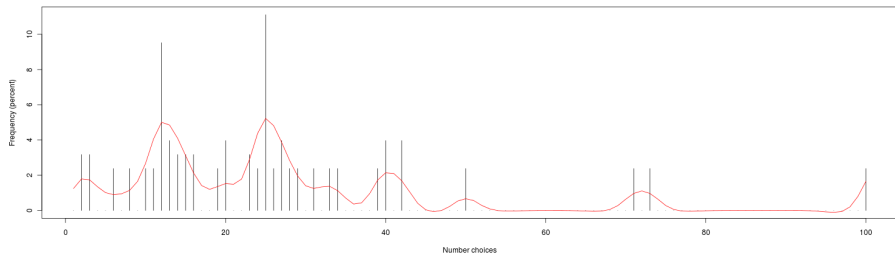
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UNIVERSITÄT  
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# The Beauty Contest

- each participant has to write down a number between 0 and 100
- all numbers are collected
- the person whose guess is closest to  $2/3$  of the arithmetic mean of all numbers submitted is the winner

# The Beauty Contest

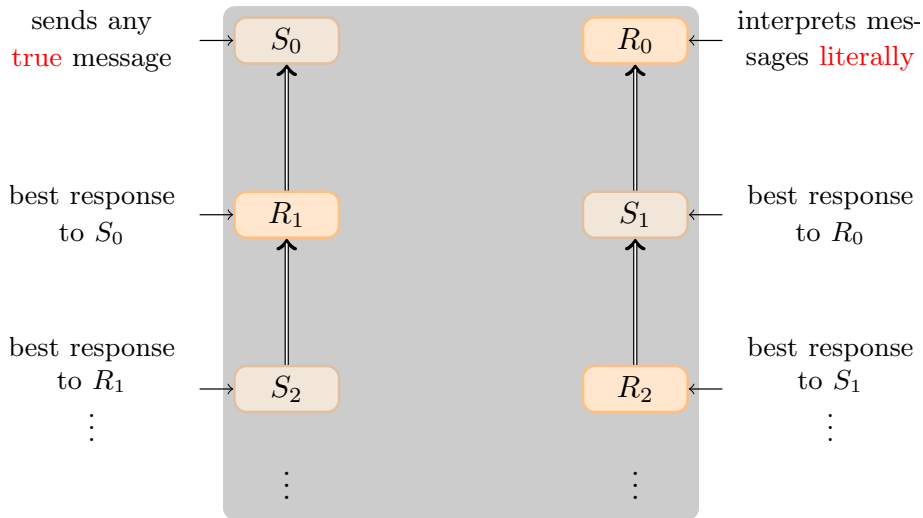


(data from Camerer 2003, *Behavioral Game Theory*)

# Signaling games

- sequential game:
  - 1 **nature** chooses a world  $w$ 
    - out of a pool of possible worlds  $W$
    - according to a certain probability distribution  $p^*$
  - 2 nature shows  $w$  to sender **S**
  - 3 S chooses a message  $m$  out of a set of possible signals  $M$
  - 4 S transmits  $m$  to the receiver **R**
  - 5 R chooses an action  $a$ , based on the sent message.
- Both S and R have preferences regarding R's action, depending on  $w$ .
- S might also have preferences regarding the choice of  $m$  (to minimize signaling costs).

# The Iterated Best Response sequence



# Quantity implicatures

- (1) a. Who came to the party?  
b. SOME: Some boys came to the party.  
c. ALL: All boys came to the party.

## Game construction

- $ct = \emptyset$
- $W = \{w_{\exists-\forall}, w_{\forall}\}$
- $w_{\exists-\forall} = \{\text{SOME}\}, w_{\forall} = \{\text{SOME}, \text{ALL}\}$
- $p^* = (1/2, 1/2)$

- interpretation function:

$$\|\text{SOME}\| = \{w_{\exists-\forall}, w_{\forall}\}$$

$$\|\text{ALL}\| = \{w_{\forall}\}$$

- utilities:

	$a_{\exists-\forall}$	$a_{\forall}$
$w_{\exists-\forall}$	1, 1	0, 0
$w_{\forall}$	0, 0	1, 1

# Truth conditions

	SOME	ALL
$w_{\exists \rightarrow \forall}$	1	0
$w_{\forall}$	1	1

## Example: Quantity implicatures

$S_0$	SOME	ALL
$w_{\exists \neg \forall}$	1	0
$w_{\forall}$	1/2	1/2

$R_1$	$w_{\exists \neg \forall}$	$w_{\forall}$
SOME	1	0
ALL	0	1

$R_0$	$w_{\exists \neg \forall}$	$w_{\forall}$
SOME	1/2	1/2
ALL	0	1

$S_1$	SOME	ALL
$w_{\exists \neg \forall}$	1	0
$w_{\forall}$	0	1

$$F = (R_1, S_1)$$

In the fixed point, SOME is interpreted as entailing  $\neg$ ALL, i.e. exhaustively.



# Lifted games

- 1 a. Ann or Bert showed up. (= OR)
  - b. Ann showed up. (= A)
  - c. Bert showed up. (= B)
  - d. Ann and Bert showed up. (= AND)
- $w_a$ : Only Ann showed up.
  - $w_b$ : Only Bert showed up.
  - $w_{ab}$ : Both showed up.

## Truth conditions

	OR	A	B	AND
$\{w_a\}$	1	1	0	0
$\{w_b\}$	1	0	1	0
$\{w_{ab}\}$	1	1	1	1
$\{w_a, w_b\}$	1	0	0	0
$\{w_a, w_{ab}\}$	1	1	0	0
$\{w_b, w_{ab}\}$	1	0	1	0
$\{w_a, w_b, w_{ab}\}$	1	0	0	0

# Lifted games

## IBR sequence: 1

$S_0$	OR	A	B	AND
$\{w_a\}$	1/2	1/2	0	0
$\{w_b\}$	1/2	0	1/2	0
$\{w_{ab}\}$	1/4	1/4	1/4	1/4
$\{w_a, w_b\}$	1	0	0	0
$\{w_a, w_{ab}\}$	1/2	1/2	0	0
$\{w_b, w_{ab}\}$	1/2	0	1/2	0
$\{w_a, w_b, w_{ab}\}$	1	0	0	0

# Lifted games

IBR sequence: 2

$R_1$	$\{w_a\}$	$\{w_b\}$	$\{w_{ab}\}$	$\{w_a, w_b\}$	$\{w_a, w_{ab}\}$	$\{w_b, w_{ab}\}$	$\{w_a, w_b, w_{ab}\}$
OR	0	0	0	1	0	0	0
A	1	0	0	0	0	0	0
B	0	1	0	0	0	0	0
AND	0	0	1	0	0	0	0

# Lifted games

## IBR sequence: 3

$S_2$	OR	A	B	AND
$\{w_a\}$	0	1	0	0
$\{w_b\}$	0	0	1	0
$\{w_{ab}\}$	0	0	0	1
$\{w_a, w_b\}$	1	0	0	0
$\{w_a, w_{ab}\}$	1/2	1/2	0	0
$\{w_b, w_{ab}\}$	1/2	0	1/2	0
$\{w_a, w_b, w_{ab}\}$	1	0	0	0

# Lifted games

- OR is only used in  $\{w_a, w_b\}$  in the fixed point
- this means that it carries two implicatures:
  - exhaustivity: Ann and Bert did not both show up
  - ignorance: Sally does not know which one of the two disjuncts is true

# Predicting behavioral data

- *Behavioral Game Theory*: predict what real people do (in experiments), rather what they ought to do if they were perfectly rational
- one implementation (Camerer, Ho & Chong, TechReport CalTech):
  - **stochastic choice**: people try to maximize their utility, but they make errors
  - **level- $k$  thinking**: every agent performs a fixed number of best response iterations, and they assume that everybody else is less smart (i.e., has a lower strategic level)

## Stochastic choice

- real people are not perfect utility maximizers
- they make mistakes  $\rightsquigarrow$  sub-optimal choices
- still, high utility choices are more likely than low-utility ones

### Rational choice: best response

$$P(a_i) = \begin{cases} \frac{1}{|\arg_j \max u_i|} & \text{if } u_i = \max_j u_j \\ 0 & \text{else} \end{cases}$$

### Stochastic choice: (logit) quantal response

$$P(a_i) \propto e^{\lambda u_i}$$

# Stochastic choice

- $\lambda$  measures degree of rationality
- $\lambda = 0$ :
  - completely irrational behavior
  - all actions are equally likely, regardless of expected utility
- $\lambda \rightarrow \infty$ 
  - convergence towards behavior of rational choice
  - probability mass of sub-optimal actions converges to 0



# Iterated Quantal Response (IQR)

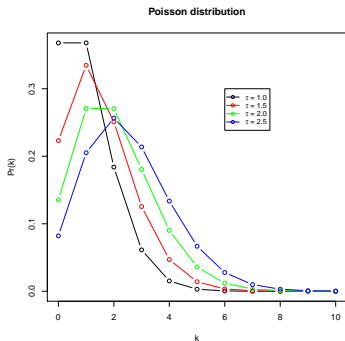
- variant of IBR model
- *best response* is replaced by *quantal response*
- predictions now depend on value for  $\lambda$
- no 0-probabilities
- IQR converges gradually

# Level- $k$ thinking

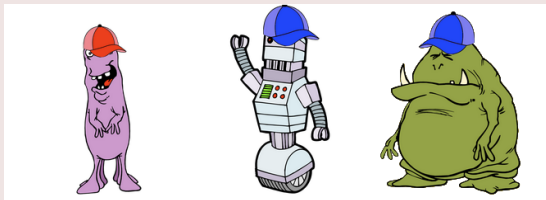
- every player:
  - performs iterated quantal response a limited number  $k$  of times (where  $k$  may differ between players),
  - assumes that the other players have a level  $< k$ , and
  - assumes that the strategic levels are distributed according to a **Poisson distribution**

$$P(k) \propto \tau^k / k!$$

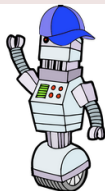
- $\tau$ , a free parameter of the model, is the average/expected level of the other players



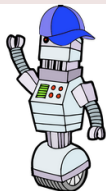
# The experimental setup



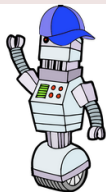
# The experimental setup



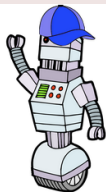
# The experimental setup










# The experimental setup










# The experimental setup



# Simple condition: Literal meanings








$S_0$				
	1/2	0	0	1/2
	0	0	1	0
	0	1/2	1/2	0








  

$R_0$			
	1	0	0
	0	0	1
	0	1/2	1/2
	1	0	0

















# Simple condition: Iterated Best Response















$R_1$			
	1	0	0
	0	0	1
	0	1	0
	1	0	0

$S_1$				
	$1/2$	0	0	$1/2$
	0	0	1	0
	0	1	0	0















# Complex condition: Literal meanings

$S_0$					$R_0$			
	0	1/2	0	1/2		1/3	1/3	1/3
	0	1/2	1/2	0		1/2	1/2	0
	0	0	0	1		0	1	0
						1/2	0	1/2

# Complex condition: Iterated Best response

$R_1$				$S_1$				
	1/3	1/3	1/3		0	1/2	0	1/2
	1/2	1/2	0		0	0	1	0
	0	1	0		0	0	0	1
	0	0	1					

# Complex condition: Iterated Best response

$S_2$					$R_2$			
	0	1	0	0		1/3	1/3	1/3
	0	0	1	0		1	0	0
	0	0	0	1		0	1	0
						0	0	1

# Experiment 1 - comprehension

- test participants' behavior in a comprehension task implementing previously described signaling games
- 48 participants on Amazon's Mechanical Turk
- two stages:
  - language learning
  - inference
- 36 experimental trials
  - 6 *simple* (one-step) implicature trials
  - 6 *complex* (two-step) implicature trials
  - 24 filler trials (entirely unambiguous/ entirely ambiguous target)

# Artificial language Zorx



XEK

1



RAV



∅

2



ZUB



KOR



∅

3

Three stages of language learning:

# Artificial language Zorx



XEK



RAV



∅



ZUB



KOR



∅

Three stages of language learning:

1

2

3



Next word

# Artificial language Zorx



XEK



RAV



∅



ZUB



KOR



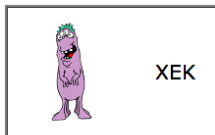
∅

Three stages of language learning:

1

2

3



Next word



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XEK



RAV



∅



ZUB



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∅

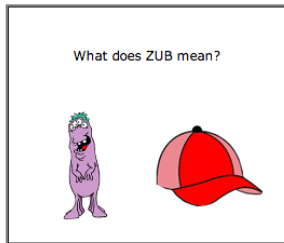
Three stages of language learning:

1



Next word

2



3

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XEK



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∅



ZUB



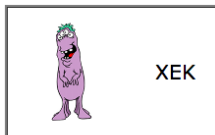
KOR



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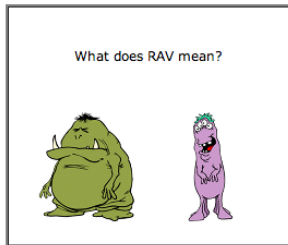
Three stages of language learning:

1



Next word

2



3

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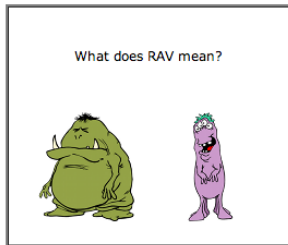
Three stages of language learning:

1

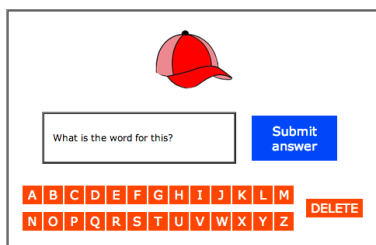


Next word

2



3



# Artificial language Zorx



XEK



RAV



∅



ZUB



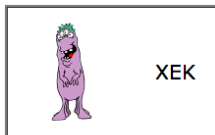
KOR



∅

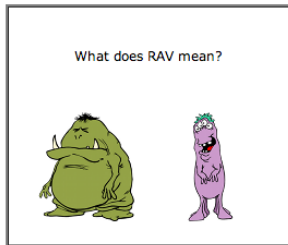
Three stages of language learning:

1

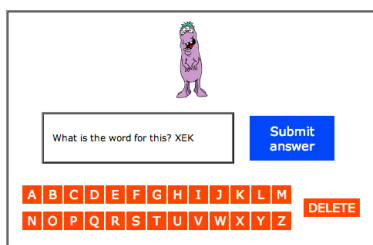


Next word

2



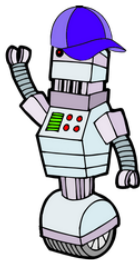
3



# Inference trial

The previous participant said:

XIR

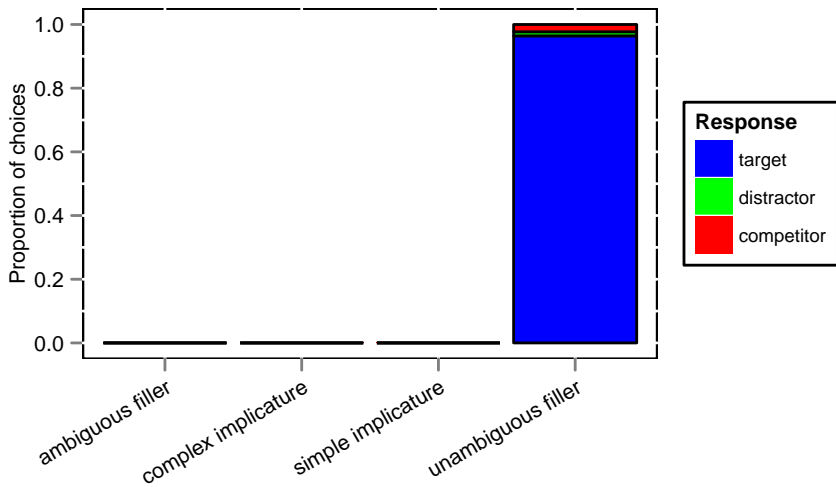


**Click on the creature you think  
the previous participant  
intended you to pick.**

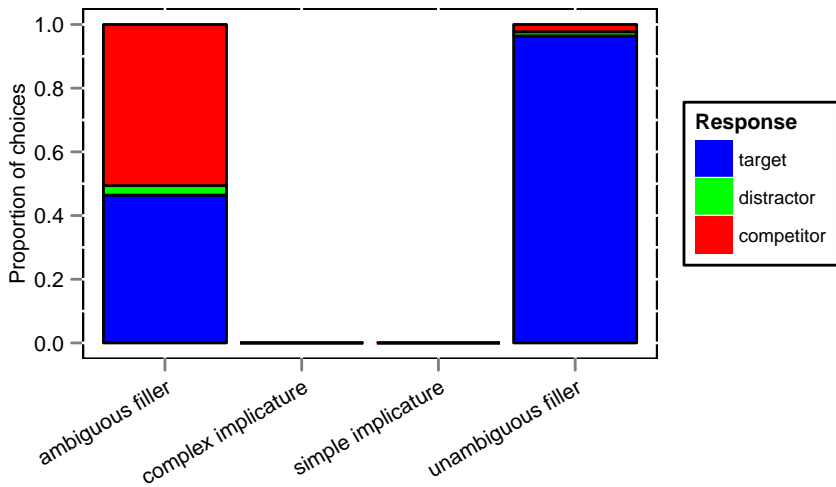
Remember the participant could  
only say one of these things:



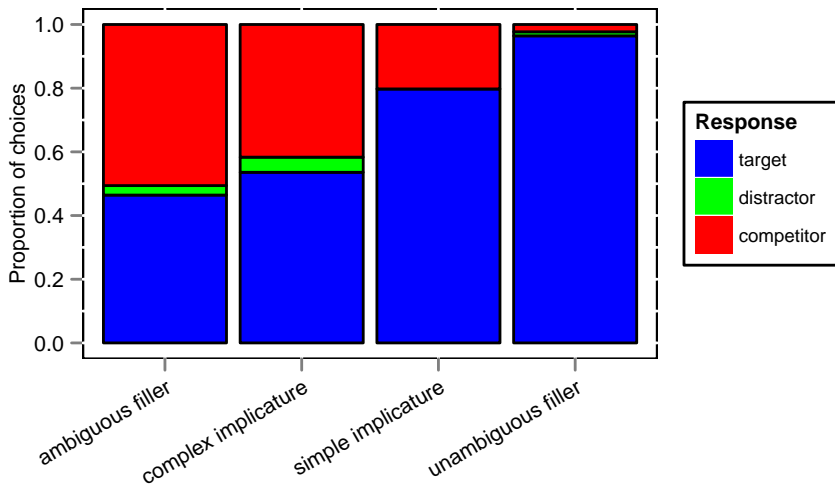
## Results - proportion of responses by condition



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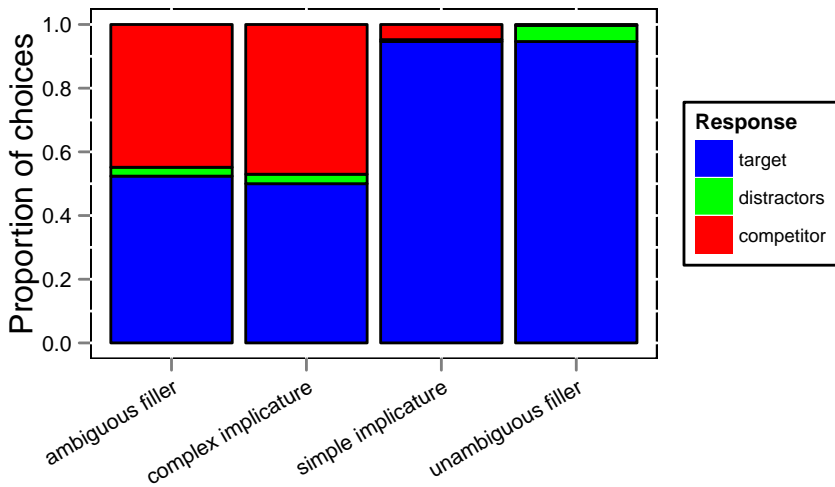




## Experiment 2 - production

- test participants' behavior in a production task implementing previously described signaling games
- 48 participants on Amazon's Mechanical Turk
- two stages:
  - language learning
  - inference
- 36 experimental trials
  - 6 *simple* (one-step) implicature trials
  - 6 *complex* (two-step) implicature trials
  - 24 filler trials (entirely unambiguous/ entirely ambiguous target)

## Results - proportion of responses by condition



## Experiment 3 - varying message costs

- Question 1: Are comprehenders aware of message costs?
- Question 2: If a cheap ambiguous message competes with a costly unambiguous one, do we find quantity implicatures, and if so, how does its likelihood depend on message costs?
- 240 participants on Amazon's Mechanical Turk
- three stages:
  - language learning
  - cost estimation
  - inference (18 trials, 6 inference and 12 filler trials)

# Extended Zorx

cheap messages



XEK



RAV



ZUB



KOR

costly messages



XAB  
BAZU  
BAZUZE

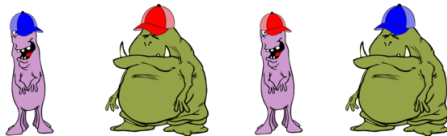


BAZ  
XABI  
XABIKO

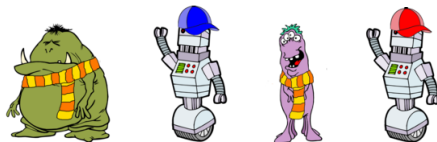
no cost  
low cost  
high cost

# Cost estimation

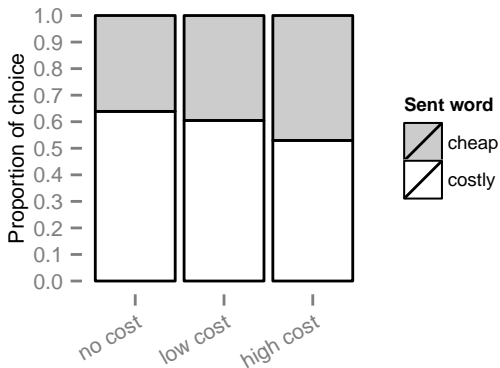
two cheap features



one cheap & one costly feature










## Results - proportion of costly messages










The use of costly messages decreases as the cost of that message increases.

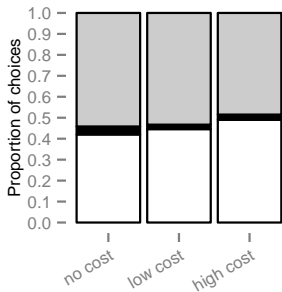
# Simple condition: Literal meanings

$S_0$				
	1/2	0	0	1/2
	0	0	1	0
	0	3/4	1/4	0

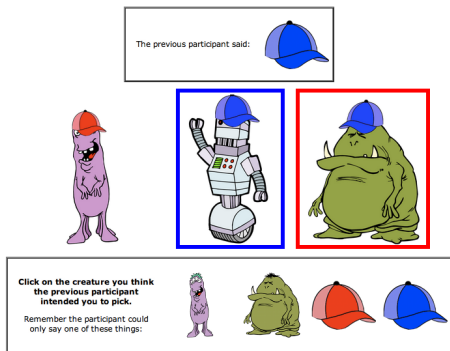
$R_0$			
	1	0	0
	0	0	1
	0	1/2	1/2
	1	0	0

# Inference results



**Response**

- target
- distractor
- competitor



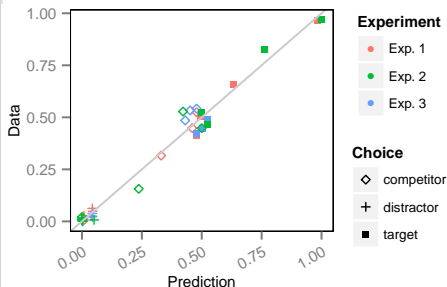
The Quantity inference becomes more likely as the cost of the ambiguous message increases.



# Model fitting

## Fitted parameters

- cost estimation: mixed effects logistic regression on the data from experiment 3
- reasoning parameters fitted via least squares regression:
  - comprehension (experiments 1, 3)  
 $\lambda = 4.825, \tau = 0.625, r = 0.99$
  - production (experiment 2)  
 $\lambda = 8.853, \tau = 0.818, r = 0.99$



# Conclusion

- proof of concept: game theoretic model captures experimental data quite well
- both speakers and listeners routinely perform simple inference steps
- likelihood of nested inferences is rather low
- speakers behave more strategically than listeners

# Collaborators

